

A SIMPLE MODEL OF HORIZONTAL FDI

Economics of European Integration, Marius Brühlhart

Assume a firm with an international monopoly for the good it produces (e.g. through patent protection). There are two countries, H and P, and demand in each country can be described with the same isoelastic demand function:

$$P_i = L_i^{-\alpha} Q_i^{\alpha}; \quad 0 < \alpha < 1;$$

$$Q_i = L_i P_i^{\frac{1}{1-\alpha}}; \quad (1)$$

where $i \in \{H, P\}$, L_i is population size and Q_i is the quantity sold. We assume that country H is bigger than country P, i.e. $L_H > L_P$.

The firm can produce with a per-plant fixed cost of f (hence with increasing returns to plant scale) and a marginal cost c_i . We assume that the marginal production cost is higher in country H than in country P, i.e. $c_H > c_P$, while the fixed cost is the same in both countries. We also assume that the overall cost-revenue configuration is such that the firm finds it profitable to produce.

(Note the analogy between the EU's centre and periphery and countries H and P, given that H has a bigger market and P has lower production costs.)

Trade between the two countries is costly. Specifically, the cost of sending one unit of the good from one country to the other is t .

The firm has three strategies:

- A: produce in H and P for the local markets
- B: produce in H and export to P
- C: produce in P and export to H

Given the demand function (1), marginal revenue is given by:

$$MR_i = P_i(1 - \alpha):$$

The firm maximises profits in each market by choosing output levels such that $MR_i = c_i$. Marginal costs for the three strategies are:

- A: $f(c_H; c_P)g$
- B: $f(c_H; (c_H + t))g$
- C: $f(c_P + t; c_P)g$

As an example, compute the firm's profit if it decides to serve market H from a production plant in H (i.e. it adopts strategy A or B). We then have:

$$P_H(1 - \alpha) = c_H;$$

$$P_H = c_H(1 - \alpha)^{-1};$$

Substituting in (1), we obtain:

$$Q_H = L_H c_H^{-\frac{1}{\sigma}} (1 - \alpha)^{\frac{1}{\sigma}};$$

Variable profit (not considering fixed costs) is given by:

$$\pi_H = (P_H - c_H)Q_H = c_H \alpha (1 - \alpha)^{-1} Q_H;$$

$$\pi_H = \alpha (1 - \alpha)^{\frac{1}{\sigma} - 1} L_H c_H^{1 - \frac{1}{\sigma}};$$

$$\pi_H = \alpha^{\frac{\sigma}{\sigma - 1}} L_H c_H^{\frac{\sigma - 1}{\sigma}}; \quad \alpha = (1 - \alpha)^{\frac{1}{\sigma} - 1};$$

Hence, total profits for the three strategies are as follows:

$$A: \quad \pi^A = \alpha^{\frac{\sigma}{\sigma - 1}} L_H c_H^{\frac{\sigma - 1}{\sigma}} + L_P c_P^{\frac{\sigma - 1}{\sigma}} - f$$

$$B: \quad \pi^B = \alpha^{\frac{\sigma}{\sigma - 1}} L_H c_H^{\frac{\sigma - 1}{\sigma}} + L_P (c_H + t)^{\frac{\sigma - 1}{\sigma}} - f$$

$$C: \quad \pi^C = \alpha^{\frac{\sigma}{\sigma - 1}} L_H (c_P + t)^{\frac{\sigma - 1}{\sigma}} + L_P c_P^{\frac{\sigma - 1}{\sigma}} - f$$

The location decision of this (potential) multinational firm is thus a function of market size, location-specific costs plant-specific fixed costs and trade costs. As trade costs t are lowered, the dominant strategy is likely to move from A to B to C.