

# INTERNATIONAL DUOPOLY AND RECIPROCAL DUMPING

*Economics of European Integration, Marius Brühlhart*

Assume a single homogeneous good  $x$ , a single production factor  $L$  and two identical countries  $i = \{H, F\}$ .

Demand in each country is given by an isoelastic function:

$$x_i = \frac{1}{2} p_i^{-\frac{1}{\varepsilon}}, \quad 0 < \varepsilon < 1, \quad \sigma = \frac{1}{\varepsilon}. \quad (1)$$

$\sigma$  is the absolute value of the price elasticity of demand for  $x$ .

There is a monopoly firm in each country. Both firms have identical production technologies featuring a fixed cost  $f$  and a constant marginal cost  $c$ . Total cost functions are thus given by:

$$TC_{x_i} = f + cx_i.$$

In **autarky**, each firm only sells on the domestic market, maximising the following profit function:

$$\pi_{x_i} = p_i x_i - cx_i - f.$$

Profits are maximised where MR equals MC. MR is:

$$\begin{aligned} \text{MR}_{x_i} &= \frac{\partial(p_i x_i)}{\partial x_i} = \frac{p_i \partial x_i + x_i \partial p_i}{\partial x_i} = p_i + x_i \frac{\partial p_i}{\partial x_i} \\ &= p_i + \frac{x_i p_i}{p_i} \frac{\partial p_i}{\partial x_i} = p_i \left( 1 + \frac{\partial p_i / p_i}{\partial x_i / x_i} \right) \\ &= p_i \left( 1 - \frac{1}{\sigma} \right) = p_i (1 - \varepsilon) \end{aligned} \quad (2)$$

Hence, choose  $x_i$  so as to satisfy:

$$\text{MR}_{x_i} = p_i (1 - \varepsilon) = c = \text{MC}_{x_i},$$

so that:

$$p_i = \left( \frac{1}{1 - \varepsilon} \right) c.$$

Therefore, price exceeds MC by a factor  $1/(1 - \varepsilon)$ .

With perfectly **free trade** among  $H$  and  $F$ , demand becomes:

$$x = p^{-\frac{1}{\varepsilon}}, \quad (3)$$

where:

$$x = x_H + x_F = \frac{1}{2}p_H^{-\frac{1}{\varepsilon}} + \frac{1}{2}p_F^{-\frac{1}{\varepsilon}}.$$

Assume Cournot competition among the two firms in the integrated market. That means that each firm chooses its profit-maximising  $x_i$  assuming that the output of the other firm will remain unchanged. The profit function of each firm is now given by:

$$\pi_{x_i} = px_i - cx_i - f,$$

or, substituting from eq.(3):

$$\pi_{x_i} = x^{-\varepsilon}x_i - cx_i - f.$$

Profits are maximised where *perceived* MR equals MC. Assuming an integrated world market (consisting of the two countries), and remembering eq. (2), we have that  $MR_x = p + x\frac{\partial p}{\partial x}$ , so that

$$MR_{x_i} = p + x_i\frac{\partial p}{\partial x}\frac{\partial x}{\partial x_i}. \quad (4)$$

With Cournot conjectures, firms assume  $\frac{\partial x}{\partial x_i} = 1$ . If we multiply the r.h.s. of eq. (4) by  $\frac{x}{x}$  and by  $\frac{p}{p}$ , we find the profit-maximising condition:

$$p\left(1 - \varepsilon\frac{x_i}{x}\right) = c,$$

which, given perfect symmetry between firms, becomes:

$$p\left(1 - \frac{\varepsilon}{2}\right) = c.$$

Since  $1/(1-\varepsilon/2) < 1/(1-\varepsilon)$ , the monopoly mark-up is lower with free trade than in autarky. This can be achieved even without any trade occurring!

Assume now that even after abolition of visible trade barriers among  $H$  and  $F$ , some **trade costs**  $t$  per unit of output remain. Assume also that the monopoly price in autarky is higher than  $c + t$ . In this setting, the MC of the domestic supplier is no longer equal to that of the exporter, and hence their equilibrium conditions are no longer identical. A home firm's profit maximisation rule is:

$$p\left(1 - \varepsilon\left[\frac{x_{HH}}{x_{HH} + x_{FH}}\right]\right) = c;$$

while that of a foreign firm is:

$$p \left( 1 - \varepsilon \left[ \frac{x_{FH}}{x_{HH} + x_{FH}} \right] \right) = c + t,$$

where  $x_{FH}$  is the quantity produced in  $F$  and sold in  $H$ .

Due to the home firm's cost advantage in  $H$ , market shares are no longer identical:

$$\frac{x_{FH}}{x_{HH} + x_{FH}} < \frac{1}{2} < \frac{x_{HH}}{x_{HH} + x_{FH}}.$$

In this setting, producers have an incentive to penetrate the market of the foreign country by setting export prices (net of  $t$ ) that are lower than prices on the home market. This is because perceived MR from foreign sales is relatively high. Exporting therefore takes place whenever it yields a perceived MR that is higher than  $c + t$ . This leads to intra-industry trade ("reciprocal dumping").